



e-ISSN: 2278-8875
p-ISSN: 2320-3765

International Journal of Advanced Research

in Electrical, Electronics and Instrumentation Engineering

Volume 14, Issue 11, November 2025

ISSN INTERNATIONAL
STANDARD
SERIAL
NUMBER
INDIA

Impact Factor: 8.807

📞 9940 572 462

📞 6381 907 438

✉ ijareeie@gmail.com

@ www.ijareeie.com



Characteristics of Optimal Wavelength Selection for the Quadrispectral Pyrometer in the Near-Infrared Spectral Range Made for Austenization of Steels

RATIANARIVO Paul Ezekel, RASTEFANO Elisée

Professor, Dept. of Electronic Engineering, ESP Antsirabe, Université de Vakinankaratra, Madagascar

Professor, Dept. of Electronic Engineering, ESPA, Université d'Antananarivo, Madagascar

ABSTRACT: The characteristics of selecting optimal wavelengths for a four-spectrum pyrometer used during the austenitizing of steels will be examined at the end of this article. Thanks to one of the physical properties of hot steels, which has the ability to radiate, its surface temperature can be measured remotely. This temperature is proportional to the emitted infrared radiation. The system is equipped with optical filters to filter the four spectra and converge them towards the respective detectors.

Steel is among the metals with nonlinear emissivity. To overcome this nonlinearity, the model called TNL.Tabc, or Temperature by Nonlinear Model, with T, a, b, and c being the parameters to be estimated, will be used to select the optimal wavelengths. It will focus on minimizing a cost function using the least squares method. With this model, we will sequentially choose the optimal wavelengths one after the other using an inverse method, which consists of fixing the temperature and finding the wavelength corresponding to that temperature. The first wavelength obtained will be used to calculate the second. This principle will be applied to find the second, third, and fourth wavelengths. Each wavelength must be tested against various criteria to minimize measurement errors in the temperature.

KEYWORDS: Multi Spectral Pyrometer, Wavelength, Infrared Radiation, Temperature, Steel, Austenization

I. INTRODUCTION

Temperature is a very essential physical quantity in manufacturing. Most of the time, thermometers are used to measure it, placing the object in direct contact with the temperature being measured. However, this technique is completely unsuitable for moving objects, objects located in hazardous areas, objects with poor thermal conductivity, objects with deformable surfaces, and especially for very high temperatures. Steels are known for their significant nonlinear selective emissivity. The metallurgical industries are particularly affected by these problems, for example, in the heat treatment of metals. The Quadri spectral pyrometer is among the best solutions for overcoming these issues. This is why the multispectral method is adopted for wavelength selection in the design of such a pyrometer.

II. LAW OF ELECTROMAGNETIC RADIATION

2.1 LAW OF PLANCK

Given a black body at temperature, we can calculate the energy density of its radiation. The calculations rely on the assumption that the electromagnetic field within the black body's limited cavity is equivalent to a set of independent harmonic oscillators in thermodynamic equilibrium at temperature T and obeying Boltzmann statistics. It can be shown that the black body's radiance is equal to the energy density of the radiation multiplied by λ , where radiance is the ratio of the luminous intensity, or energy density, of the radiation to the emitting surface area.

Consider a black body at temperature T , we can calculate the energy density of the radiation from this body. The calculations rely on the assumption that the electromagnetic field in the limited cavity of the black body is equivalent to a set of independent harmonic oscillators in thermodynamic equilibrium at temperature T and obeying Boltzmann statistics. It can be shown that the radiance $L_{\lambda}^0(T)$ of the black body is equal to the energy density of the radiation



multiplied by $\frac{4\pi}{c}$, where the radiance is the ratio of the luminous intensity or energy density of the radiation to the emitting surface.

$$L_{\lambda}^0(T) = \frac{2hc^2\lambda^{-5}}{\exp\left(\frac{hc}{k\lambda T}\right) - 1}$$

where $h = 6,6255 \times 10^{-34}$ Js is constant of Planck, $k = 1,38 \times 10^{-23}$ JK⁻¹ constante of Boltzmann, $c = 2,996 \times 10^8$ ms⁻¹ is the speed of electromagnetic waves in a vacuum.

This formula is also used with the so-called Planck constants C_1 and C_2 :

$$L_{\lambda}^0(T) = \frac{C_1\lambda^{-5}}{\exp\left(\frac{C_2}{\lambda T}\right) - 1} \quad \text{whith } C_1 = 2hc^2 \quad \text{and } C_2 = \frac{hc}{k}$$

2.2. DIFFERENT REGIONS OF THE INFRARED SPECTRUM

The infrared range is relatively broad, covering wavelengths from 0.8 μm to 1000 μm . Within this wavelength range, three regions are generally distinguished: near-infrared, mid-infrared, and far-infrared. The near-infrared spectrum lies between wavelengths of 0.8 μm and 2.5 μm .

2.3. DEFINITION OF SPECTRAL EMISSIVITY

The ratio between the monochromatic luminance of the real source $L_{\lambda}(T)$ and that of the black body $L_{\lambda}^0(T)$, for the same values of wavelength λ and temperature T , defines the monochromatic emissivity or spectral emissivity ε_{λ} of the source.

$$\varepsilon_{\lambda} = \frac{L_{\lambda}(T)}{L_{\lambda}^0(T)}$$

In general, spectral emissivity depends on the source, wavelength λ , temperature T , and direction of emission. The total emissivity, on the other hand, is defined by the following relationship:

$$\varepsilon_t = \int_0^{\infty} \varepsilon_{\lambda} d\lambda$$

The luminance of a black body does not depend on the direction of emission, and if the same is true for the real source (radiating source according to Lambert's law), the spectral emissivity also does not depend on the direction of emission.

2.4. SPECTRAL EMISSIVITY OF METALS

The wavelength dependence of emissivity can be expressed in several forms, but we will consider those that can fit experimental measurements or simplify the analysis. Most surfaces have emissivity that varies with wavelength and temperature. The emissivity of metallic surfaces in the visible and near-infrared wavelengths often exhibits a polynomial wavelength dependence.

$$\varepsilon_{\lambda} = c_0 + c_1\lambda + c_2\lambda^2 + \dots + c_n\lambda^n$$

In our case, we use the second-order polynomial model: $\varepsilon_{\lambda} = a + b\lambda + c\lambda^2$

But in theory, emissivity depends on the material, the nature of its surface, the temperature, the wavelength, and possibly the measurement setup used. In the fig.1, since metals often reflect radiation, they are generally characterized by a low,



nonlinear degree of emission, highly dependent on the surface structure and tending towards longer wavelengths. This dependence can lead to different and unreliable measurement results.

When selecting appropriate thermal measuring instruments, care should be taken to ensure that the infrared radiation is measured at a specific wavelength and within a temperature range where the metals exhibit a relatively high degree of emission.

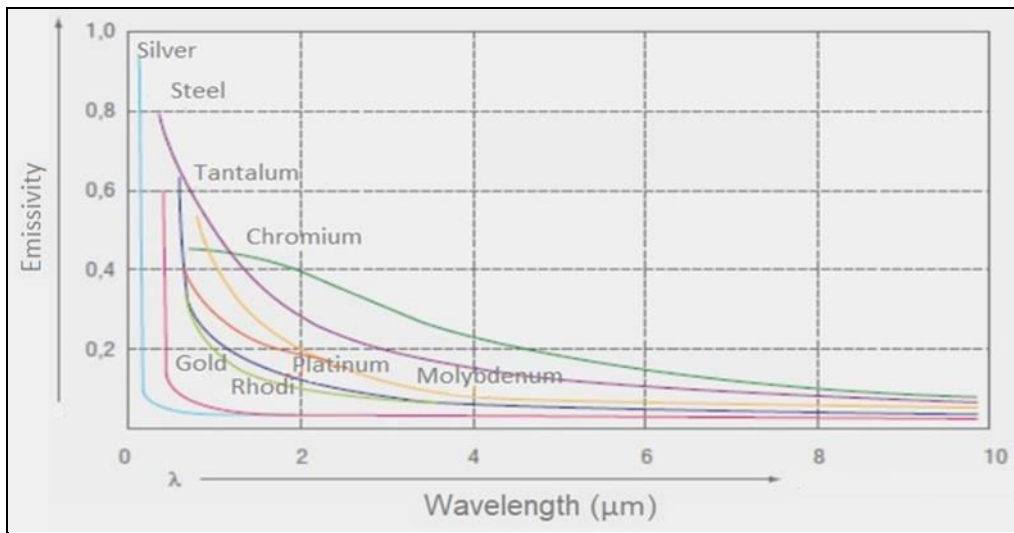


Fig.1 Spectral emission degree of metals

2.5. AUSTENITIZATION OF STEELS

The purpose of austenitization is to dissolve carbon and, possibly, precipitated alloying elements in the form of carbides. To achieve this, it is necessary to create conditions where carbon is soluble in iron, that is, to induce, through heating, the transformation of iron into iron. In the Fig. 2, the austenitization temperature range is between 1000.15K and 1421.15K.

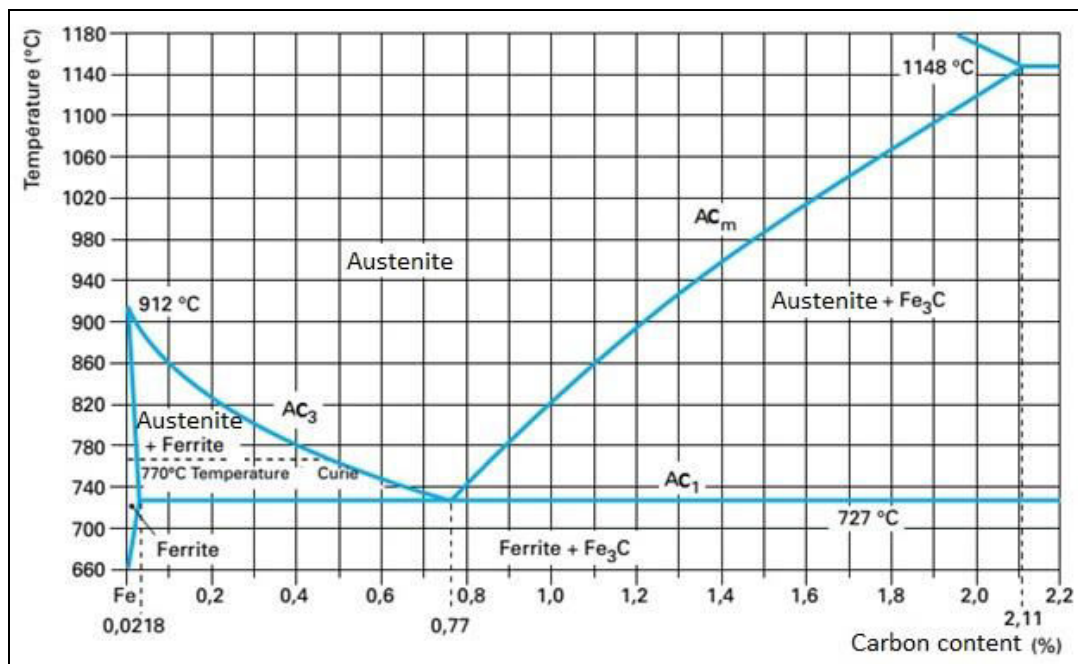


Fig. 2 FeC diagram of the steel domain



In the context of mass heat treatment, austenitization comprises two steps:
 - Heating to the so-called austenitization temperature;
 - Holding at this temperature.

III. MULTI-SPECTRAL METHOD BASED ON PLANCK'S LAW

3.1.PRINCIPLE OF QUAD SPECTRAL PYROMETER

In the fig.3 The radiation from the source is filtered by optical systems which allow the four different spectra to pass through and converge them respectively towards the four identical detection systems.

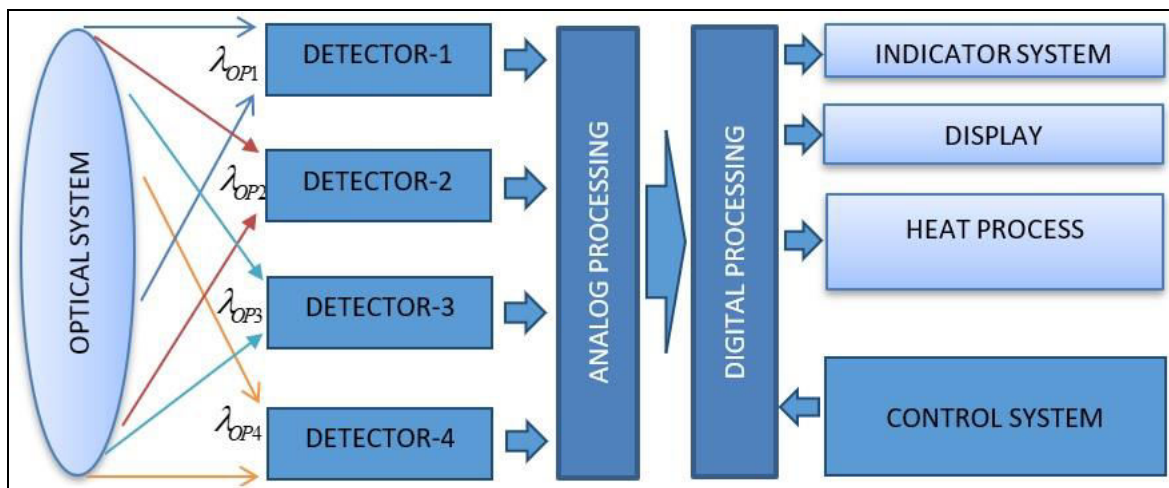


Fig. 3 General principle of quadrispectral pyrometers

3.2.PRESENTATION OF THE TNL.TABC MODEL

The goal is to determine the temperature of the steel during heat treatment along with its emissivity. The model "TNL.Tabc" stands for Temperature by Nonlinear Model, where T, a, b, and c are the parameters to be estimated. This model is unbiased and based on estimating fluxes expressed using Planck's law. It will also incorporate polynomial modeling of the emissivity up to the second order of the overall spectral transfer function of the measurement chain using coefficients (a, b, c). The flux as a function of wavelength and temperature is given by $L_{\lambda}(T, a, b, c)$

$$L_{\lambda}(T, a, b, c) = (a + b\lambda_i + c\lambda_i^2) \frac{C_1 \lambda_i^{-5}}{\exp\left(\frac{C_2}{\lambda_i T}\right) - 1}$$

Whith $\epsilon_{\lambda} = a + b\lambda_i + c\lambda_i^2$ the spectral emissivity.

The estimation of the parameters $\{T, a, b, c\}$ will then be carried out by minimizing the function $J(T, a, b, c)$, in which $L_{\lambda_i}^{exp}$ designates the experimental spectral flux measured at the wavelength λ_i , and $L_{\lambda_i}(T, a, b, c)$ is the theoretical spectral flux at the wavelength λ_i .

$$J(T, a, b, c) = \sum_{i=1}^4 (L_{\lambda_i}^{exp} - L_{\lambda_i}(T, a, b, c))^2$$

$$J(T, a, b, c) = (L_{\lambda_1}^{exp} - L_{\lambda_1}(T, a, b, c))^2 + \dots + (L_{\lambda_4}^{exp} - L_{\lambda_4}(T, a, b, c))^2$$

Note : The subscript 4 designates the four (04) wavelengths for estimating the four parameters $\{T, a, b, c\}$. So we have four (04) equations for the theoretical flows $L_{\lambda_1}(T, a, b, c), L_{\lambda_2}(T, a, b, c), L_{\lambda_3}(T, a, b, c)$ et $L_{\lambda_4}(T, a, b, c)$.



3.3. MODEL FOR THE SEQUENTIAL WAVELENGTH SELECTION METHOD

The method used for temperature estimation is based on minimizing a cost function using a least-squares method. With this method, we will define the optimal wavelengths using the inverse method. This method involves fixing the temperature and finding the wavelength corresponding to that temperature. These wavelengths minimize the standard deviation of the estimated temperature. The determination of the various optimal wavelengths will be performed using the cost function $J(T, a, b, c)$ associated with the "TNL.Tabc" model.

The statistical properties of the parameter estimator associated with the TNL.Tabc model and the parameters provided by the least squares method are given by the variance-covariance matrix. Using this matrix, we can determine the standard deviations σ_β of the different parameters, and in particular, that of temperature σ_T . The TNL.Tabc model is a nonlinear model; therefore, we will use the approximate expression of the ordinary least squares variance-covariance matrix, which is given for a parameter vector $\beta = (T, a, b, c)$, under the assumption of additive, independent, identically distributed noise (constant variance σ_{noise}^2 and zero mean), by:

$$\text{cov}(\beta) = \begin{bmatrix} \sigma_T^2 & \text{cov}(T, a) & \text{cov}(T, b) & \text{cov}(T, c) \\ \text{cov}(T, a) & \sigma_a^2 & \text{cov}(a, b) & \text{cov}(a, c) \\ \text{cov}(T, b) & \text{cov}(a, b) & \sigma_b^2 & \text{cov}(b, c) \\ \text{cov}(T, c) & \text{cov}(a, c) & \text{cov}(b, c) & \sigma_c^2 \end{bmatrix} = (X^t X)^{-1} \sigma_{noise}^2$$

And the standard deviation on the temperature σ_T is given as a function of the standard deviation of the noise σ_{noise} , by:

$$\sigma_T = \sqrt{(X^t X)^{-1}} \sigma_{noise}$$

With X the sensitivity matrix associated with the variance-covariance matrix, defined by :

$$X = \begin{bmatrix} \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial c} \\ \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial c} \\ \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial c} \\ \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial c} \end{bmatrix}$$

The standard deviation of the noise will be taken to be the value obtained experimentally with the infrared camera, and having a value of $\sigma_{noise} \approx 8,97.10^4 Wm^{-2}$, that is $7,43.10^{-3} \%$ of the maximum of Planck's law.

3.4. PSEUDO-OPTIMAL METHOD FOR WAVELENGTH SELECTION

The pseudo-optimal method consists of sequentially selecting wavelengths while respecting all the different criteria. These wavelengths are those that minimize the standard deviation of the temperature at a fixed temperature, thus finding the temperature range for the heat treatment of steels. In our case, we will use a fixed design temperature (T_F) of 1073.15K, 1173.15K, 1223.15K, 1273.15K, and 1373.15K.

Selection of the first optimal wavelengths



The method of sequential selection of "pseudo-optimal" wavelengths consists of choosing for the first wavelength filter λ_{OP1} , the one which minimizes the standard deviation σ_T on the temperature, assuming that the measurement is mono spectral. The cost function $J(\beta)$ consists of only one parameter : the temperature T.

$$J(T) = \left(L_{\lambda_1}^{exp} - L_{\lambda_1}(T, a, b, c) \right)^2$$

The temperature T is then the only parameter to estimate. The sensitivity matrix X is composed only of the first column and first row.

$$X = \left[\frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial T} \right]$$

The minimization of the cost function $J(T)$, involves the sensitivity matrix X of the flux at the various parameters to be estimated. The first optimal wavelength λ_{OP1} will minimize this standard deviation.

Selection of the second optimal wavelengths

The selection of the second filter is performed by setting $a = 1$, $b = 1$, and $\lambda_1 = \lambda_{OP1}$. And looking for second wavelength, the shortest that minimizes the local standard deviation of temperature in the $TNL.Ta$ model. The function cost $J(T, a)$ and the sensitivity matrix X are respectively composed as follows:

$$J(T, a) = \sum_{i=1}^2 \left(L_{\lambda_i}^{exp} - L_{\lambda_i}(T, a, b, c) \right)^2 = \left(L_{\lambda_1}^{exp} - L_{\lambda_1}(T, a, b, c) \right)^2 + \left(L_{\lambda_2}^{exp} - L_{\lambda_2}(T, a, b, c) \right)^2$$

$$X = \begin{bmatrix} \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial a} \\ \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial a} \end{bmatrix}$$

Selection of the third optimal wavelengths

For the third wavelength, it is obtained by minimizing the cost function $J(T, a, b)$ with the sensitivity matrix X associated with the model $TNL.Tab$ by fixing $\lambda_1 = \lambda_{OP1}$ and $\lambda_2 = \lambda_{OP2}$.

$$J(T, a, b) = \sum_{i=1}^3 \left(L_{\lambda_i}^{exp} - L_{\lambda_i}(T, a, b, c) \right)^2 = \left(L_{\lambda_1}^{exp} - L_{\lambda_1}(T, a, b, c) \right)^2 + \dots + \left(L_{\lambda_3}^{exp} - L_{\lambda_3}(T, a, b, c) \right)^2$$

$$X = \begin{bmatrix} \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial b} \\ \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial b} \\ \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial b} \end{bmatrix}$$

Selection of the fourth and last optimal wavelengths

The fourth optimal wavelength will be obtained on the same principle as how to obtain the second and the third optimal wavelength by fixing $a = 1$, $b = 1$, $c = 1$, $\lambda_1 = \lambda_{OP1}$, $\lambda_2 = \lambda_{OP2}$ and $\lambda_3 = \lambda_{OP3}$. The cost function $J(T, a, b, c)$ and the sensitivity matrix X associated with the model $TNL.Tabc$ are respectively represented as follows:

$$J(T, a, b, c) = \sum_{i=1}^4 \left(L_{\lambda_i}^{exp} - L_{\lambda_i}(T, a, b, c) \right)^2 = \left(L_{\lambda_1}^{exp} - L_{\lambda_1}(T, a, b, c) \right)^2 + \dots + \left(L_{\lambda_4}^{exp} - L_{\lambda_4}(T, a, b, c) \right)^2$$



$$X = \begin{bmatrix} \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_1}(T, a, b, c)}{\partial c} \\ \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_2}(T, a, b, c)}{\partial c} \\ \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_3}(T, a, b, c)}{\partial c} \\ \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial T} & \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial a} & \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial b} & \frac{\partial L_{\lambda_4}(T, a, b, c)}{\partial c} \end{bmatrix}$$

IV. CRITERIA FOR SELECTING THE OPTIMAL WAVELENGTHS

Our pyrometer must be very sensitive to the temperature between 975.15 °K and 1473.15 °K. This range borders the temperature range of the heat treatment of steels which is between 1000.15 °K and 1421.15 °K [8]. So that we can have better optimal wavelengths, we will try to find optimal wavelengths from the temperature set (TS) at 1073.15 °K, 1173.15 °K, 1223.15 °K, 1273.15 °K and 1373.15 °K.

1. PYROMETER SPECTRAL RANGE CRITERION

Our first criterion for selecting optimal wavelengths is the spectral range of our pyrometer, which operates in the band between 0.8µm and 2.5µm. Measuring the temperature of a metal requires the use of short wavelengths to avoid the relative error due to emissivity.

Table.1 Optimal wavelengths pre-selected according to the pyrometer's spectral range

Tc[K]	Channel 1		Channel 2		Channel 3		Channel 4	
	λ_{OP1} [µm]	σ_T [K]	λ_{OP2} [µm]	σ_T [K]	λ_{OP3} [µm]	σ_T [K]	λ_{OP4} [µm]	σ_T [K]
1073.15	2.246	0.000959	1.535	0.005373	1.186	0.043606	0.967	0.461628
							1.392	0.471311
					1.945	0.038898	2.000	0.132117
							1.099	0.128315
1173.15	2.054	0.000671	1.403	0.003772	1.085	0.030674	1.719	0.484844
							2.122	0.659303
					1.778	0.027332	0.884	0.323962
							1.273	0.333100
1223.15	1.970	0.000568	1.346	0.003185	1.041	0.025831	1.896	0.090029
							1.821	0.075742
					1.707	0.023056	1.005	0.090259
							1.572	0.340205
1273.15	1.893	0.000684	1.294	0.002712	1	0.022004	1.939	0.465602
							0.848	0.272897
					1.640	0.019644	1.222	0.279541
							0.965	0.075973
1373.15	1.755	0.000357	1.199	0.002005	0.927	0.016302	1.509	0.287155
							1.088	0.176781
					1.520	0.014494	1.749	0.064520
							0.900	0.065571
							1.449	0.244430
							1.788	0.334194
							0.756	0.172321
							1.622	0.047746
							0.855	0.047922
							1.343	0.180200
							1.658	0.245986



Multispectral measurement minimizes error, therefore choosing a short wavelength gives better accuracy on temperature. We observe that each time a wavelength is added, the standard deviation deteriorates by about a factor of 10. So with this method, the more the number of spectra increases, the measurement error also increases, whereas our goal is to minimize it as much as possible.

4.2. CRITERIA FOR THE MINIMUM DIFFERENCE BETWEEN TWO SUCCESSIVE WAVELENGTHS

To avoid amplifying the measurement error, while remaining as close as possible to minimize the measurement error due to the spectral variation of the emissivity, the minimum difference between the two successive wavelengths must be respected.

$$\Delta_{Min} \lambda_{ji} = |\lambda_j - \lambda_i| > \frac{T \lambda_j^2}{C_2} \Big|_{\lambda_j > \lambda_i}$$

The minimum difference between the first and second wavelengths will therefore be:

$$\lambda_{OP1} - \lambda_{OP2} \geq \Delta_{Min} \lambda_{1-2}$$

The second maximum wavelength will be selected according to this relationship:

$$\lambda_{OP2Max} \leq \lambda_{OP1} - \Delta_{Min} \lambda_{1-2}$$

The difference between the second and third wavelengths will therefore be:

$$\lambda_{OP2} - \lambda_{OP3} \geq \Delta_{Min} \lambda_{2-3}$$

The maximum value of the third wavelength is then:

$$\lambda_{OP3Max} \leq \lambda_{OP2} - \Delta_{Min} \lambda_{2-3}$$

The same principle applies to the last and fourth optimal wavelength:

$$\lambda_{OP3} - \lambda_{OP4} \geq \Delta_{Min} \lambda_{3-4}, \lambda_{OP4Max} \leq \lambda_{OP3} - \Delta_{Min} \lambda_{3-4}$$

The four optimal wavelengths selected respecting the criterion of minimum standard deviation on temperature and minimum difference between two successive wavelengths, for a temperature of 1073.15K, 1173.15K, 1223.15K, 1273.15K and 1373.15K will be represented in table.2.

In the infrared measurement, the standard deviation cannot exceed 5%. The largest values were obtained for the shortest wavelength and for wavelengths affected by atmospheric absorption. In the other infrared spectral ranges, the standard deviation between the first and last spectra was less than 2%.

Table.2 Optimal wavelength obtained from 1073.15K, 1173.15K, 1223.15K, 1273.15K and 1373.15K according to the criterion of $\Delta_{min} \lambda$



T _C [K]	λ_{OP} [μm]	σ_T [K]	σ_T [%]	$\Delta\lambda$ [μm]	$\Delta_{min}\lambda$ [μm]
1073.15	$\lambda_{OP1} = 2.246$	0.000959	0.000089	$\lambda_{OP1} - \lambda_{OP2} = 0.711$	$\lambda_{OP1} - \lambda_{OP2} = 0.411$
	$\lambda_{OP2} = 1.535$	0.005373	0.000501	$\lambda_{OP2} - \lambda_{OP3} = 0.349$	$\lambda_{OP2} - \lambda_{OP3} = 0.192$
	$\lambda_{OP3} = 1.186$	0.043606	0.004063	$\lambda_{OP3} - \lambda_{OP4} = 0.219$	$\lambda_{OP3} - \lambda_{OP4} = 0.114$
	$\lambda_{OP4} = 0.967$	0.461628	0.043016		
1173.15	$\lambda_{OP1} = 2.054$	0.000671	0.000057	$\lambda_{OP1} - \lambda_{OP2} = 0.651$	$\lambda_{OP1} - \lambda_{OP2} = 0.344$
	$\lambda_{OP2} = 1.403$	0.003772	0.000321	$\lambda_{OP2} - \lambda_{OP3} = 0.318$	$\lambda_{OP2} - \lambda_{OP3} = 0.160$
	$\lambda_{OP3} = 1.085$	0.030674	0.002614	$\lambda_{OP3} - \lambda_{OP4} = 0.201$	$\lambda_{OP3} - \lambda_{OP4} = 0.095$
	$\lambda_{OP4} = 0.884$	0.323962	0.027614		
1223.15	$\lambda_{OP1} = 1.970$	0.000568	0.000046	$\lambda_{OP1} - \lambda_{OP2} = 0.624$	$\lambda_{OP1} - \lambda_{OP2} = 0.329$
	$\lambda_{OP2} = 1.346$	0.003185	0.000260	$\lambda_{OP2} - \lambda_{OP3} = 0.305$	$\lambda_{OP2} - \lambda_{OP3} = 0.154$
	$\lambda_{OP3} = 1.041$	0.025831	0.002112	$\lambda_{OP3} - \lambda_{OP4} = 0.193$	$\lambda_{OP3} - \lambda_{OP4} = 0.092$
	$\lambda_{OP4} = 0.848$	0.272897	0.022311		
1273.15	$\lambda_{OP1} = 1.893$	0.000684	0.000054	$\lambda_{OP1} - \lambda_{OP2} = 0.599$	$\lambda_{OP1} - \lambda_{OP2} = 0.317$
	$\lambda_{OP2} = 1.294$	0.002712	0.000213	$\lambda_{OP2} - \lambda_{OP3} = 0.294$	$\lambda_{OP2} - \lambda_{OP3} = 0.148$
	$\lambda_{OP3} = 1.000$	0.022004	0.001728	$\lambda_{OP3} - \lambda_{OP4} = 0.185$	$\lambda_{OP3} - \lambda_{OP4} = 0.088$
	$\lambda_{OP4} = 0.815$	0.232649	0.018273		
1373.15	$\lambda_{OP1} = 1.755$	0.000357	0.000026	$\lambda_{OP1} - \lambda_{OP2} = 0.556$	$\lambda_{OP1} - \lambda_{OP2} = 0.293$
	$\lambda_{OP2} = 1.199$	0.002005	0.000146	$\lambda_{OP2} - \lambda_{OP3} = 0.272$	$\lambda_{OP2} - \lambda_{OP3} = 0.119$
	$\lambda_{OP3} = 0.927$	0.016302	0.001187	$\lambda_{OP3} - \lambda_{OP4} = 0.171$	$\lambda_{OP3} - \lambda_{OP4} = 0.082$
	$\lambda_{OP4} = 0.756$	0.172321	0.012549		

We observe that only one group of optimal wavelengths, obtained from each calculation temperature, meets the criterion of minimum distance between two successive optimal wavelengths.

Furthermore, the minimum required distance between two wavelengths is proportional to the longer of the two successive wavelengths.

We also note that all groups of optimal wavelengths with the lowest standard deviations fail to meet the criterion of minimum distance between two successive wavelengths.

From the temperature 1373.15K, the optimal wavelengths begin to enter to the visible region ($\lambda_{OP4} = 0.756 \mu\text{m}$), so the measurable temperature in the near-infrared spectral band does not exceed this value.

4.3.STANDARD DEVIATION ON THE TEMPERATURE FROM THE TEMPERATURE RANGE OF THE FLUXES OBTAINED FROM THE OPTIMAL WAVELENGTHS

In the table-3, verification of the standard deviation of optimal wavelengths is almost necessary to know the errors on the temperature in the entire temperature range from 975.15K to 1473.15K of the austenization of steels.

Table.3 Standard deviation on temperature σ_T [K] from the pyrometer spectral range of optimal wavelengths obtained

T _C [K]	λ_{OP} [μm]	Gamme de température du pyromètre						
		975.15K	1073.15K	1173.15K	1223.15K	1273.15K	1373.15K	1473.15K
1073.15	$\lambda_{OP1} = 2.246$	0.001459	0.000959	0.000686	0.000595	0.000524	0.000420	0.000349
	$\lambda_{OP2} = 1.535$	0.003146	0.001559	0.000884	0.000693	0.000555	0.000378	0.000273
	$\lambda_{OP3} = 1.186$	0.011394	0.004336	0.001977	0.001408	0.001033	0.000600	0.000379
	$\lambda_{OP4} = 0.967$	0.056348	0.016485	0.006042	0.003911	0.002627	0.001305	0.000719
1173.15	$\lambda_{OP1} = 2.054$	0.001582	0.000982	0.000671	0.000571	0.000493	0.000382	0.000310
	$\lambda_{OP2} = 1.403$	0.004541	0.002068	0.001094	0.000832	0.000648	0.000419	0.000290
	$\lambda_{OP3} = 1.085$	0.021317	0.007281	0.003035	0.002078	0.001471	0.000801	0.000478
	$\lambda_{OP4} = 0.884$	0.138194	0.035367	0.011602	0.007152	0.004595	0.002106	0.001084
1223.15	$\lambda_{OP1} = 1.970$	0.001674	0.001011	0.000675	0.000568	0.000486	0.000371	0.000296
	$\lambda_{OP2} = 1.346$	0.005532	0.002417	0.001235	0.000925	0.000711	0.000448	0.000304
	$\lambda_{OP3} = 1.041$	0.029580	0.009576	0.003817	0.002564	0.001782	0.000940	0.000546
	$\lambda_{OP4} = 0.848$	0.219035	0.052467	0.016292	0.009805	0.006161	0.002715	0.001351



1273.15	$\lambda_{OP1} = 1.893$	0.001789	0.001050	0.000685	0.000571	0.000484	0.000343	0.000286
	$\lambda_{OP2} = 1.294$	0.006791	0.002847	0.001406	0.001038	0.000786	0.000484	0.000321
	$\lambda_{OP3} = 1.000$	0.041610	0.012759	0.004862	0.003202	0.002185	0.001116	0.000631
	$\lambda_{OP4} = 0.815$	0.349686	0.078430	0.023061	0.013551	0.008329	0.003529	0.001697
1373.15	$\lambda_{OP1} = 1.755$	0.002101	0.001164	0.000725	0.000592	0.000492	0.000357	0.000274
	$\lambda_{OP2} = 1.199$	0.010626	0.004095	0.001886	0.001350	0.000995	0.000582	0.000370
	$\lambda_{OP3} = 0.927$	0.084590	0.023272	0.008105	0.005130	0.003377	0.001616	0.000863
	$\lambda_{OP4} = 0.756$	0.917752	0.180401	0.047544	0.026628	0.015659	0.006132	0.002754

We have four (4) optimal wavelengths that respect the minimum difference between two (2) successive wavelengths for a given temperature. As the calculation temperature increases up to 1373.15 K, the optimal wavelengths decrease to at least 0.140 μm .

We also observe that the standard deviation of the temperature improves as the measurement temperature increases. Therefore, temperature errors decrease for measurements at high temperatures.

As the wavelength decreases, the standard deviation deteriorates, i.e., it increases ($T_C=1223.15\text{K}$: $\lambda_{OP1} = 1.970\mu\text{m}$, $\lambda_{OP2}=1.346 \mu\text{m}$, $\lambda_{OP3} = 1.041 \mu\text{m}$, $\lambda_{OP4} = 0.848 \mu\text{m}$. If we apply these wavelengths to $T=1073.15\text{K}$, we have respectively a standard deviation of 0.001011K, 0.002417K, 0.001023K, 0.052467K).

The standard deviation deteriorates rapidly if the wavelength exceeds the lower limit of the near-infrared range ($\lambda_{OP4} = 0.756 \mu\text{m}$ calculated from the temperature at $T_C = 1373.15\text{K}$; the standard deviations at this wavelength for the temperature range of our pyrometer are at $T = 975.15\text{K} \rightarrow \sigma_T = 0.917752\text{K}$ and at $T = 1473.15\text{K} \rightarrow \sigma_T = 0.002754\text{K}$).

The temperature range of our pyrometer is from 975.15K to 1473.15K. We observe that the optimal wavelengths obtained at $T_C = 1073.15 \text{ K}$ have a lower standard deviation compared to those obtained at $T_C = 1373.15 \text{ K}$. The worst standard deviation is 0.056348K at $T=975.15\text{K}$ for $T_C=1073.15\text{K}$, while it is 0.917752K at $T=975.15\text{K}$ for $T_C=1373.15\text{K}$. Therefore, the standard deviation increases, meaning the measurement error increases, as the wavelength decreases and the temperature being measured becomes significant.

4.3. SENSITIVITY OF THE FLUX TO TEMPERATURE AND WAVELENGTH

The model called TNL.Tabc involves taking temperature measurements without fully controlling all influencing factors. However, certain precautions must be taken to minimize measurement error in temperature. Our working range lies on the increasing portion of the Planck curve because the reduced sensitivities of the flux to temperature χ_T and wavelength χ_λ are enhanced at shorter wavelengths.

$$\chi_T = \frac{1}{L_\lambda(T)} \frac{dL_\lambda(T)}{dT}, \quad \chi_\lambda = \frac{1}{L_\lambda(T)} \frac{dL_\lambda(T)}{d\lambda}$$

The wavelengths obtained should provide greater sensitivity to both temperature and wavelength. In table-4, we show the sensitivity of the flux obtained from the optimal wavelengths at temperature and in table-5, flux sensitivity to wavelength in the pyrometer temperature range will be presented.

Table.4 Sensitivity of the flux obtained from the optimal wavelengths at temperature

$T_C[\text{K}]$	$\lambda_{OP} [\mu\text{m}]$	Gamme de température du pyromètre						
		975.15K	1073.15K	1173.15K	1223.15K	1273.15K	1373.15K	1473.15K
1073.15	$\lambda_{OP1} = 2.246$	0.006773	0.005576	0.004674	0.004304	0.003978	0.003429	0.002990
	$\lambda_{OP2} = 1.535$	0.009898	0.008140	0.006813	0.006268	0.005786	0.004976	0.004326
	$\lambda_{OP3} = 1.186$	0.012810	0.010534	0.008815	0.008109	0.007485	0.006435	0.005591
	$\lambda_{OP4} = 0.967$	0.015711	0.012919	0.010811	0.009945	0.009179	0.007891	0.006856
1173.15	$\lambda_{OP1} = 2.054$	0.007402	0.006091	0.005102	0.004697	0.004339	0.003737	0.003255
	$\lambda_{OP2} = 1.403$	0.010829	0.008905	0.007452	0.006856	0.006328	0.005442	0.004729
	$\lambda_{OP3} = 1.085$	0.014002	0.115147	0.009635	0.008863	0.008181	0.007033	0.006111
	$\lambda_{OP4} = 0.884$	0.017186	0.014132	0.011826	0.010879	0.010041	0.008632	0.007500



1223.15	$\lambda_{OP1} = 1.970$	0.007716	0.006348	0.005317	0.004894	0.004520	0.003892	0.003389
	$\lambda_{OP2} = 1.346$	0.011287	0.009282	0.007767	0.007146	0.006596	0.005671	0.004929
	$\lambda_{OP3} = 1.041$	0.014594	0.012001	0.010042	0.009238	0.008527	0.007330	0.006369
	$\lambda_{OP4} = 0.848$	0.017916	0.014732	0.012328	0.011341	0.010467	0.008998	0.007818
1273.15	$\lambda_{OP1} = 1.893$	0.008029	0.006605	0.005531	0.005090	0.004701	0.004047	0.003522
	$\lambda_{OP2} = 1.294$	0.011741	0.009655	0.008079	0.007432	0.006861	0.005898	0.005126
	$\lambda_{OP3} = 1.000$	0.015193	0.012493	0.010454	0.009617	0.008876	0.007631	0.006630
	$\lambda_{OP4} = 0.815$	0.018641	0.015329	0.012827	0.011800	0.010891	0.009363	0.008135
1373.15	$\lambda_{OP1} = 1.755$	0.008658	0.007122	0.005962	0.005486	0.005066	0.004359	0.003792
	$\lambda_{OP2} = 1.199$	0.012671	0.010420	0.008719	0.008021	0.007403	0.006365	0.005531
	$\lambda_{OP3} = 0.927$	0.016389	0.013477	0.011277	0.010374	0.009575	0.008231	0.007152
	$\lambda_{OP4} = 0.756$	0.020096	0.016525	0.013828	0.012721	0.011741	0.010093	0.008769

The sensitivity of the flux to temperature increases as the wavelength decreases. In the spectral band of our pyrometer, the temperature sensitivity of the flux applied at a given wavelength decreases as the temperature increases. In the spectral band between 0.8 μm and 2.5 μm , the temperature sensitivity of the flux is significantly better at 975.15 K than at 1473.15 K, the upper limit of our measurement temperature. Therefore, the lower the measurement temperature, the better the temperature sensitivity of the flux.

Table.5 Flux sensitivity to wavelength in the pyrometer temperature range

T_c [K]	λ_{OP} [μm]	Pyrometer temperature range						
		975.15K	1073.15K	1173.15K	1223.15K	1273.15K	1373.15K	1473.15K
1073.15	$\lambda_{OP1} = 2.246$	708783	438419	215437	118132	28815.5	-129307	-264699
	$\lambda_{OP2} = 1.535$	3017940	2433730	1949550	1737360	1541990	1194490	894948
	$\lambda_{OP3} = 1.186$	6295360	5315970	4503650	4147350	3819100	3234490	2729580
	$\lambda_{OP4} = 0.967$	10640700	9167330	7945180	7409060	6915060	6035040	5274610
1173.15	$\lambda_{OP1} = 2.054$	1072800	748273	480169	363010	255370	64539.6	-99164.8
	$\lambda_{OP2} = 1.403$	3947540	3247910	2667830	2413500	2179270	1762380	1402700
	$\lambda_{OP3} = 1.085$	7950900	6780620	5809910	5384100	4991770	4292950	3689210
	$\lambda_{OP4} = 0.884$	13263700	11500700	10038200	9396680	8805530	7752420	6842330
1223.15	$\lambda_{OP1} = 1.970$	1273700	920437	628392	500698	383333	175134	-3618.14
	$\lambda_{OP2} = 1.346$	4446190	3685950	3055540	2779110	2524490	2071220	1680020
	$\lambda_{OP3} = 1.041$	8840230	7568920	6514380	6051800	5624470	4866320	4210320
	$\lambda_{OP4} = 0.848$	14664100	12748200	11158900	10461700	9819330	8674880	7685850
1273.15	$\lambda_{OP1} = 1.893$	1486270	1103270	786471	647884	520461	294298	99976.3
	$\lambda_{OP2} = 1.294$	4965930	4143300	3461080	3161900	2886300	2395610	1971990
	$\lambda_{OP3} = 1.000$	9784980	8407280	7264470	6763160	6301240	5478390	4767390
	$\lambda_{OP4} = 0.815$	16124000	14049800	12329300	11574500	10879000	9639990	8569220
1373.15	$\lambda_{OP1} = 1.755$	1952330	1506060	1136600	974840	826027	561657	334207
	$\lambda_{OP2} = 1.199$	6114380	5156120	4361330	4012740	3691580	3119630	2625670
	$\lambda_{OP3} = 0.927$	11811500	10208300	8878370	8294970	7757400	6799760	5972200
	$\lambda_{OP4} = 0.756$	19255100	16844500	14844900	13967800	13159500	11719500	10475000

The sensitivity of flux to wavelength increases as the wavelength decreases. Therefore, measurements using wavelength spectra in the near-infrared region are highly recommended.

The flux sensitivity to wavelength of wavelengths obtained from the upper temperature range is increasingly better than that obtained at the lower limit within the temperature range to be measured.

The existence of negative values explains why the use of these wavelengths obtained at T_c between 1073.15 K and 1223.15 K, i.e., wavelengths greater than 1970 μm , can lead to significant errors if the temperature to be measured is above 1373.15 K. Therefore, these wavelengths do not cover, in terms of flux sensitivity, the temperatures required for the austenitization of steels.



V. CONCLUSION

The TNL.Tabc model, based on Planck's law, allows for the simultaneous determination of temperature and spectral emissivity. This model enabled us to sequentially select the optimal wavelengths for a multispectral pyrometer designed for the heat treatment of steels.

Among the optimal wavelengths obtained from 1073.15 K, 1173.15 K, 1223.15 K, 1273.15 K, and 1373.15 K, only a group of four wavelengths meets the criterion of minimum distance between two successive wavelengths. Therefore, selecting these wavelengths based on the minimum standard deviation is insufficient.

All the optimal wavelengths exhibit good temperature sensitivity between 975.15 K and 1473.15 K. However, the fluxes at these optimal wavelengths are not at all sensitive if the temperature is between 1373.15K and 1473.15K. In addition, their standard deviation is far from exceeding the 5% error limit.

In conclusion, only the optimal wavelengths obtained from a temperature of 1273.15 K meet all the selection criteria for the four optimal wavelengths for a multispectral pyrometer intended for the heat treatment of steels. Therefore, with the sequential least-squares method for selecting optimal wavelengths in the TNL.Tabc model, it is better to use the temperature towards the upper limit of the temperature range (975.15 K to 1473.15 K) to be measured than the temperature towards the lower limit. And the closer one gets to the upper limit, the more the wavelengths reach the visible spectrum.

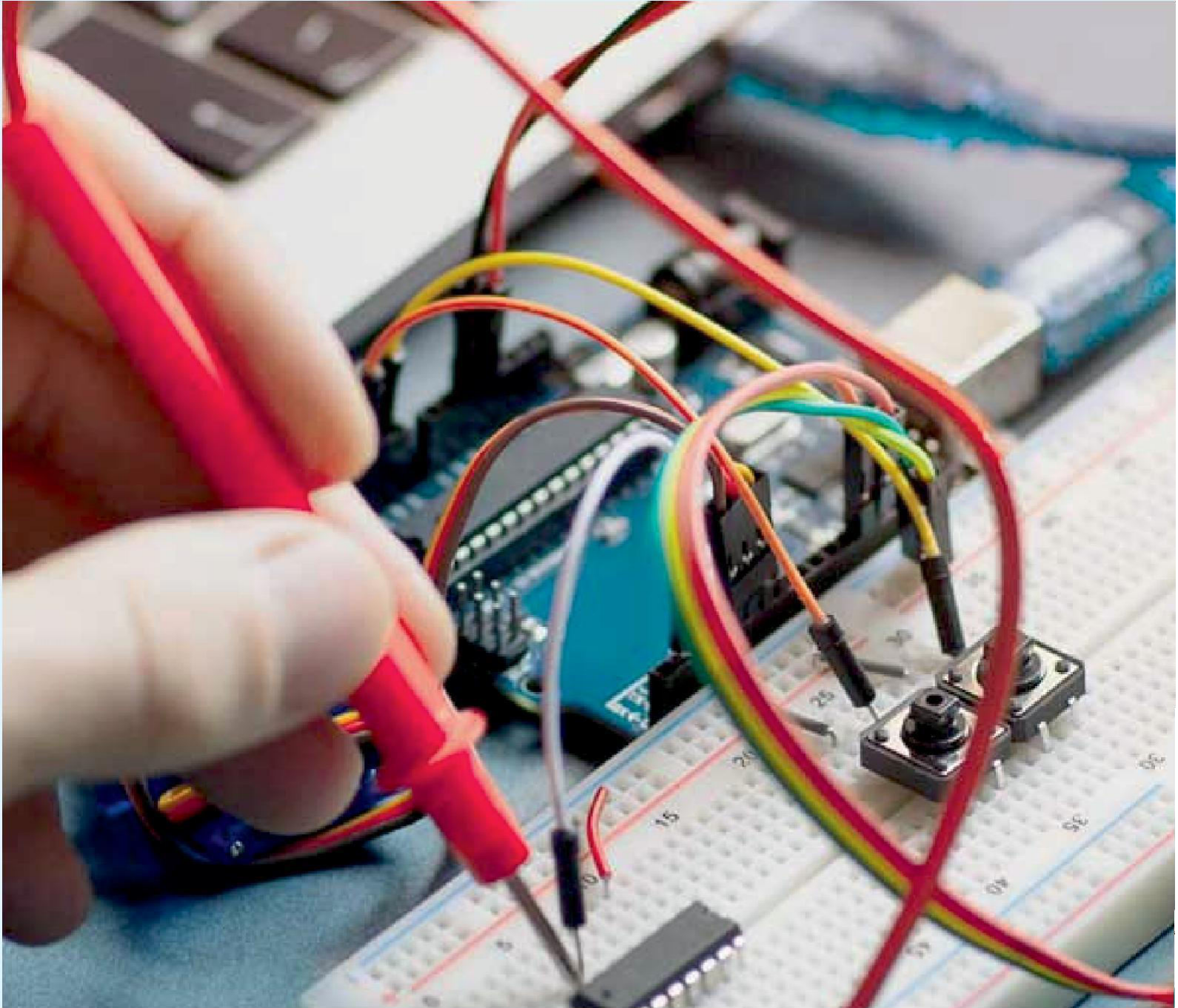
For the austenization of steels, the temperature varies approximately between 1073.15K and 1173.15K, the use of wavelengths in the near-infrared region while respecting the permeability of the area is completely recommended because all parameters such as flux sensitivity to wavelength and temperature, standard deviation on the temperature to the temperature range, the minimum difference between the two successive wavelengths are all acceptable.

REFERENCES

- [1] Philippe Herve, Julie Cedelle, Ionut Negreanu, Infrared technique for simultaneous determination of temperature and emissivity, <https://www.sciencedirect.com/science/article/pii/S1350449510000721>
- [2] Th.Duvaut, Comparison between multiwavelength infrared and visible pyrometry: Application to metals, <https://www.sciencedirect.com/science/article/pii/S1350449507001375>
- [3] Tairan Fu, Minghao Duan, Jiaqi Tang, Cong lingShi, Measurements of the directional spectral emissivity based on a radiation heating source with alternating spectral distributions, <https://www.sciencedirect.com/science/article/pii/S001793101500784X>
- [4] G. R. Gathers, Analysis of multiwavelength pyrometry using nonlinear chi-square fits and Monte Carlo methods, <https://link.springer.com/article/10.1007%2F978-1-4020-0503-8>
- [5] Helcio R.B. Orlando, Olivier Fudym, Denis Maillat, Renato M. Cotta, Thermal Measurements and Inverse Techniques, <https://www.crcpress.com/Thermal-Measurements-and-Inverse-Techniques/Orlande-Fudym-Maillet-Cotta/p/book/9781138113862>
- [6] Thomas Pierre, Benjamin Rémy, Alain Degiovanni, Microscale temperature measurement by the multispectral and statistic method in the ultraviolet-visible wavelengths, <https://aip.scitation.org/doi/10.1063/1.2826945>
- [7] M. Boivineau, G. Pottlacher, Thermophysical properties of metals at very high temperatures obtained by dynamic heating techniques: recent advances, <https://www.inderscienceonline.com/doi/pdf/10.1504/IJMPT.2006.009468>
- [8] A Barlier-Salsi, Stray light correction on array spectroradiometers for optical radiation risk assessment in the workplace, <http://iopscience.iop.org/article/10.1088/0952-4746/34/4/915/meta>
- [9] Simone MATTEI, Rayonnement thermique des matériaux opaques, publié le 10 janv. 2005, <https://www.techniques-ingenieur.fr/base-documentaire/energies-th4/transferts-thermiques-42214210/rayonnement-thermique-des-materiaux-opaques-be8210>
- [10] Tairan Fu, Jiangfan Liu, Minghao Duan, Anzhou Zong, Temperature measurements using multicolor pyrometry in thermal radiation heating environments, <https://doi.org/10.1063/1.4870252>



- [11] Christophe Rodiet, Benjamin Rémy, Alain Degiovanni , Franck Demeurie, – Optimisation of wavelengths selection used for the multi-spectral temperature measurement by ordinary least squares method of surfaces exhibiting non-uniform emissivity,
<https://www.tandfonline.com/doi/abs/10.1080/17686733.2013.812816>
- [12] Jian Xing, Shuang Long Cui, Yuan Dong Shi, A Iteration Processing Algorithm for Multi-Wavelength Pyrometer, Disponible en ligne <https://doi.org/10.4028/www.scientific.net/AMM.568-570.401>
- [13]V.TankH.Dietl, Multispectral infrared pyrometer for temperature measurement with automatic correction of the influence of emissivity,
<https://www.sciencedirect.com/science/article/pii/0020089190900492>
- [14]George Zonios, Noise and stray light characterization of a compact CCD spectrophotometer used in biomedical applications, <https://www.osapublishing.org/ao/abstract.cfm?URI=ao-49-2-163>
- [15]AntónioAraújo, Dual-band pyrometry for emissivity and temperature measurements of gray surfaces at ambient temperature: The effect of pyrometer and background temperature uncertainties,
<https://www.sciencedirect.com/science/article/pii/S0263224116304687>
- [16]Th.Duvaut , D.Georgeault, J.L.Beaudoin, Multiwavelength infrared pyrometry: optimization and computer simulations, <https://www.sciencedirect.com/science/article/pii/1350449595000402>
- [17]V.TankH.Dietl, Multispectral infrared pyrometer for temperature measurement with automatic correction of the influence of emissivity,
<https://www.sciencedirect.com/science/article/pii/0020089190900492>
- [18]PhilippeHerve, JulieCedelle, IonutNegreanu, Infrared technique for simultaneous determination of temperature and emissivity,
<https://www.sciencedirect.com/science/article/pii/S1350449510000721>
- [19]Christophe Rodiet, Benjamin Remy, Alain Degiovanni, Optimal wavelengths obtained from laws analogous to the Wien's law for monospectral and bispectral methods, and general methodology for multispectral temperature measurements taking into account global transfer function including non-uniform emissivity of surfaces,
<https://www.sciencedirect.com/science/article/pii/S1350449516300147>
- [20]C. RODIET, T. PIERRE, B. REMY et A. DEGIOVANNI, Mesure de température par méthode multi-spectrale dans l'Infrarouge et l'Ultraviolet, <https://www.researchgate.net/publication/265047799>
- [21]Christophe rodiet1*, Benjamin remy1, thomas pierre2 and alain degiovanni1, Influence of measurement noise and number of wavelengths on the temperature measurement of opaque surface with variable emissivity by a multi-spectral method based on the flx ratio in the infrared-ultraviolet range, <https://www.researchgate.net/publication/275030564>



INNO  SPACE
SJIF Scientific Journal Impact Factor

 **doi**[®]
cross **ref**

 **INTERNATIONAL
STANDARD
SERIAL
NUMBER
INDIA**



International Journal of Advanced Research

in Electrical, Electronics and Instrumentation Engineering

 9940 572 462  6381 907 438  ijareeie@gmail.com



www.ijareeie.com

Scan to save the contact details